How poor is the stimulus? Evaluating hierarchical generalization in neural networks trained on child-directed speech

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Abstract

When acquiring syntax, children consistently choose hierarchical rules over competing nonhierarchical possibilities. Is this preference due to a learning bias for hierarchical structure, or due to more general biases that interact with hierarchical cues in children's linguistic input? We explore these possibilities by training LSTMs and Transformers-two types of neural networks without a hierarchical biason data similar in quantity and content to children's linguistic input: text from the CHILDES corpus. We then evaluate what these models have learned about English yes/no questions, a phenomenon for which hierarchical structure is crucial. We find that, though they perform well at capturing the surface statistics of childdirected speech (as measured by perplexity), both model types generalize in a way more consistent with an incorrect linear rule than the correct hierarchical rule. These results suggest that human-like generalization from text alone requires stronger biases than the general sequence-processing biases of standard neural network architectures.

1 Introduction

Syntax is driven by hierarchical structure, yet we typically encounter sentences as linear sequences of words. How do children come to recognize the hierarchical nature of the languages they acquire? Some argue that humans must have a hierarchical inductive bias—an innate predisposition for hierarchical structure (Chomsky, 1965, 1980). An alternative view (e.g., Lewis and Elman, 2001) is that no such bias is necessary: there may be clear evidence for hierarchical structure in children's input, so that children would choose hierarchical rules even without a hierarchical bias.

At first blush, recent work in natural language processing (NLP) may seem to indicate that no hierarchical bias is necessary. Neural networks trained on naturally-occurring text perform impressively on syntactic evaluations even though they have no explicit syntactic structure built into them (e.g., Gulordava et al., 2018; Wilcox et al., 2018; Warstadt et al., 2020a). However, these results do not provide strong evidence about the learning biases required to learn language from the data available to humans because these models receive very different training data than humans do (Warstadt and Bowman, 2022). First, NLP models are typically trained on far more data than children receive, so models have more opportunities to encounter rare syntactic structures (Linzen, 2020). Second, most training sets in NLP are built from Internet text (e.g., Wikipedia), which differs qualitatively from the utterances that children typically hear; e.g., sentences in Wikipedia are on average 25 words long (Yasseri et al., 2012), compared to 5 words for sentences in the North American English subset of the CHILDES corpus of child-directed speech (MacWhinney, 2000).

In this work, to evaluate if neural networks without a hierarchical bias generalize like children do, we train models on text¹ comparable to the sentences in children's linguistic input: English data from CHILDES. We then analyze what they have learned about the relationship between declarative sentences, such as (1a), and their corresponding yes/no questions, such as (1b):

(1) a. Those <u>are</u> your checkers.b. <u>Are</u> those your checkers?

Crucially, nearly all naturally-occurring yes/no questions are consistent with two rules: one based

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¹Section 6.5 discusses other input types (e.g., visual input).

on hierarchical structure (2), and one based on linear order (3):^{2,3}

- (2) HIERARCHICALQ: The auxiliary at the start of a yes/no question corresponds to the **main** auxiliary of the corresponding declarative.
- (3) LINEARQ: The auxiliary at the start of a yes/no question corresponds to the **first** auxiliary of the corresponding declarative.

Despite the scarcity of evidence disambiguating these rules, children reliably favor HIERARCHI-CALQ (Crain and Nakayama, 1987), albeit with occasional errors consistent with LINEARQ (Ambridge et al., 2008). Yes/no questions thus are a prime candidate for an aspect of English syntax for which human-like generalization requires a hierarchical bias. We evaluate yes/no question performance in LSTMs and Transformers, two neuralnetwork architectures that have no inherent hierarchical inductive bias (McCoy et al., 2020; Petty and Frank, 2021). These architectures employ different computational mechanisms, so consistent results across both would indicate that our results are not due to idiosyncrasies of one particular architecture.

To investigate if models generalize more consistently with the hierarchical or linear rule, we evaluate them on cases where the rules make different predictions, such as (4): under HIERARCHI-CALQ, the question that corresponds to (4a) is (4b), whereas under LINEARQ it is (4c).

(4) a. The boy who has talked <u>can</u> read.
b. <u>Can</u> the boy who has talked <u>read</u>?
c. *Has the boy who <u>talked can</u> read?

We find that across several ways of framing the learning task, models fail to learn HIERARCHI-CALQ. Instead, they generalize in ways that depend on linear order and on the identities of specific words. These results suggest that children's training data, if taken to be words alone, may not contain enough hierarchical cues to encourage hierarchical generalization in a learner without a hierarchical bias. Thus, explaining human acquisition of syntax may require postulating that humans have stronger inductive biases than those of LSTMs and Transformers, or that information other than word sequences plays a crucial role.⁴

2 Background

Though HIERARCHICALQ and LINEARQ often make the same predictions, the evidence in children's input may still favor HIERARCHICALQ. The most straightforward evidence would be utterances that directly disambiguate the rules, such as (4b). Pullum and Scholz (2002) show that disambiguating examples appear in the *Wall Street Journal*, in literature, and arguably in child-directed speech, but direct evidence may still be too rare to robustly support HIERARCHICALQ (Legate and Yang, 2002). Nonetheless, children might conclude that yes/no questions obey HIERARCHI-CALQ rather than LINEARQ based on *indirect* evidence—evidence that *other* syntactic phenomena are hierarchical (Mulligan et al., 2021).

To test if the cues favoring HIERARCHICALQ render a hierarchical bias unnecessary, we study how well non-hierarchically-biased models acquire English yes/no questions. Several prior papers have used this approach, but their training data differed from children's input in important ways: some used synthetic datasets (Lewis and Elman, 2001; Frank and Mathis, 2007; Clark and Eyraud, 2007; McCoy et al., 2020), others used massive Internet corpora (Lin et al., 2019; Warstadt and Bowman, 2020), and those that used child-directed speech simplified the data by replacing each word with its part of speech (Perfors et al., 2011; Bod et al., 2012). We used training data closer to children's input, namely sentences from CHILDES with word identities preserved, rather than being converted to parts of speech. Two other recent works have also trained neural networks on CHILDES data (Pannitto and Herbelot, 2020; Huebner et al., 2021), but neither investigated yes/no questions.

One particularly important reason for training models on CHILDES is that, in prior work, different types of training data have yielded diverging results: Recent models trained on synthetic data failed to properly acquire yes/no questions (McCoy et al., 2020; Petty and Frank, 2021), whereas ones trained on large Internet corpora scored well on evaluations of yes/no questions (Lin et al., 2019; Warstadt and Bowman, 2020). Given these differing results, it is not clear from past work how these

²In past work these rules have been framed as transformations named MOVE-FIRST and MOVE-MAIN (McCoy et al., 2020). We instead follow Berwick et al. (2011) and frame the child's knowledge as a relationship between sentences.

³Though these two rules are the most prominent in prior literature, other rules are possible; see Section 5.2.

⁴GitHub repo with data and code: https://github.com/ adityayedetore/lm-povstim-with-childes.

models would generalize when faced with the type of data that children receive.

3 Overview of Experimental Setup

We evaluated models on yes/no questions in two ways. First, we used relative acceptability judgments (Experiment 1): We trained neural networks on the task of language modeling (predicting the next word at every point in the sentence) and evaluated whether they assigned a higher probability to sentences consistent with LINEARQ or HIERAR-CHICALQ. Our second approach was based on text generation (Experiment 2): We trained networks to take in a declarative sentence and output the corresponding question, and tested whether they generalized in a way more consistent with LIN-EARQ or HIERARCHICALQ. Under both framings, we trained models on data from CHILDES and evaluated them on targeted datasets constructed to differentiate LINEARQ and HIERARCHICALQ.

4 Experiment 1: Relative Acceptability

4.1 Dataset

To train models on data as similar as possible to the sentences children receive, we extracted data from CHILDES (MacWhinney, 2000). We used the North American English portion. We wished to replicate children's *input*, so we excluded the children's own utterances, leaving a 9.6-millionword corpus. We allocated 90% of the data to training, 5% to validation, and 5% to testing. We replaced words that appeared two or fewer times in the training set with <unk>, giving a replacement rate of 0.3%. See Appendix A for more details.

4.2 Task: Next-Word Prediction

We trained models on next-word prediction, also known as language modeling. We chose this task for two reasons. First, it is clear empirically that next-word prediction can teach neural networks a substantial amount about syntax (e.g., Hu et al., 2020). Second, it is plausible that humans perform some version of next-word prediction during sentence processing (Altmann and Kamide, 1999; Hale, 2001; Levy, 2008; Kutas et al., 2011) and that such prediction may play a role in acquisition (Elman, 1991). Thus, while next-word prediction is certainly not the only goal of human language learners, we view this task as a reasonable first step in emulating human language acquisition.

4.3 Architectures

We used two neural network architectures: LSTMs (Hochreiter and Schmidhuber, 1997) and Transformers (Vaswani et al., 2017). We chose these models for two reasons. First, they have been the most successful architectures in NLP. Thus, we have reason to believe that, of the types of low-bias models invented, these two are the ones most likely to discover linguistic regularities in our CHILDES training data. Second, the two architectures process sequences very differently (via recurrence vs. via attention). Thus, if both generalize similarly, we would have evidence that what was learned is strongly evidenced in the data, rather than due to a quirk of one particular architecture.

For our LSTMs, we used 2 layers, a hidden and embedding size of 800, a batch size of 20, a dropout rate of 0.4, and a learning rate of 10. For our Transformers, the corresponding values were 4, 800, 10, 0.2, and 5, and we used 4 attention heads. We chose these values based on a hyperparameter search described in Appendix B. All following results are averaged across 10 runs with different random seeds.

4.4 Results: Language Model Quality

Before testing models on questions, we used perplexity to evaluate how well they captured the basic structure of their training domain. As a baseline, we used a 5-gram model with Kneser-Ney smoothing (Kneser and Ney, 1995) trained with KenLM (Heafield, 2011). The test set perplexity for the 5-gram baseline was 24.37, while the average test set perplexity for the LSTMs and Transformers was 20.05 and 19.69, respectively. For perplexity, lower is better. Thus, both neural network types outperformed the strong baseline of a smoothed 5-gram model, showing that they performed well at capturing the basic statistics of their training domain.⁵

4.5 General Syntactic Evaluation

As an additional way to check the validity of our setup, we evaluated our models on the Zorro dataset (Huebner et al., 2021), which is based on BLiMP (Warstadt et al., 2020a). Zorro contains 24 evaluations, each of which targets one syntactic phenomenon (e.g., subject-verb agreement) and involves sentence pairs for which one sentence is grammatical, and the other is minimally different

⁵For an intuitive illustration of our model quality, see the sample text generated by them in Appendix H.

but ungrammatical (e.g., by violating subject verb agreement). A model is said to get a sentence pair correct if it assigns a higher probability to the grammatical sentence than the ungrammatical one. Huebner et al. (2021) showed that Transformers trained on CHILDES data can perform well on many of the Zorro categories, so if our setup is sound, our own models should also perform well on Zorro.

See Appendix D for full results. For each syntactic phenomenon, most model re-runs scored above 0.9, though at least one scored near the chance level of 0.5. For each re-run of each architecture there is at least one phenomenon for which the model scores over 0.97, and many models score 1.00 on some phenomena. Thus, all models score well on at least some syntactic evaluations, attaining results comparable to those of Huebner et al. (2021) and providing additional support for the validity of our setup. We now test whether these models have also successfully learned the specific phenomenon that we focus on, yes/no questions—a phenomenon not included in the Zorro dataset.

4.6 Yes/No Questions

Evaluation Dataset: Forced-Choice Acceptability Judgments As a first way to test whether our models have learned HIERARCHICALQ, we evaluate whether they assign higher probabilities to sentences consistent with HIERARCHICALQ than to minimally different sentences that are ungrammatical. For this purpose, we create an evaluation dataset containing groups of 6 questions, each created by starting with a declarative sentence, such as (5), and then deleting the **first**, **main**, or neither auxiliary, and inserting the **first** or **main** auxiliary at the front of the sentence.⁶ For instance, in (6b), the **first** auxiliary has been preposed, and the **main** auxiliary has been deleted.

- (5) The dog who has seen a boy <u>did</u> try.
- (6) a. **Has** the dog who seen a boy \underline{did} try?
 - b. **Has** the dog who **has** seen a boy try?
 - c. Has the dog who has seen a boy did try?
 - d. **<u>Did</u>** the dog who seen a boy <u>**did**</u> try?
 - e. **<u>Did</u>** the dog who **has** seen a boy try?
 - f. <u>Did</u> the dog who has seen a boy <u>did</u> try?

Within each group, we evaluate which question the model assigned the highest probability to. If a model has correctly learned HIERARCHICALQ, it should assign the highest probability to the question consistent with this rule, such as (6e).

Several past papers about yes/no questions have used the same general approach (Lewis and Elman, 2001; Reali and Christiansen, 2005). However, these papers considered only pairs of sentences, whereas we consider groups of 6 to allow for a wider range of possible generalizations that a model might have learned.

To generate the declaratives from which we formed groups of 6 questions, we used the contextfree grammar (CFG) in Appendix F, which has a vocabulary selected from the most common words in CHILDES. Each declarative generated by the CFG (e.g., (5)) contains two auxiliary verbs: one before the sentence's main verb and one inside a relative clause modifying the subject. One potential problem is that some questions are consistent with both HIERARCHICALQ and LINEARQ. For instance, (7a) can be formed from (7b) with the HIERARCHI-CALQ-consistent steps PREPOSE-MAIN,DELETE-MAIN, or from (7c) with the LINEARQ-consistent steps PREPOSE-FIRST,DELETE-MAIN.

- (7) a. Did the boy who did see the person laugh?
 - b. The boy who did see the person did laugh.
 - c. The boy who did see the person can laugh.

To avoid this problem, we required that the auxiliary before the main verb must select for a different verb inflection than the one in the relative clause. For instance in (5), **did** selects for the verb's bare form, while **has** selects for the past participle form. Thus, the auxiliary at the start of the question could only correspond to whichever auxiliary in the declarative has the same selectional properties.⁷

Results: Relative Question Acceptability For each sentence group, we used per-word perplexity to see which of the 6 candidates the models scored most highly.⁸ For both LSTMs and Transformers, the correct category (PREPOSE MAIN, DELETE MAIN) was the second-rarest choice, and

⁶It would be possible to also use a 'prepose other' category, where an auxiliary not in the input is inserted (McCoy et al., 2018). We excluded this category because using it would raise complications about which 'other' auxiliary to choose.

 $^{^{7}}$ A model could succeed on this dataset with a rule that relates the auxiliary at the start of a question with the *last* auxiliary in the declarative form. Since our models fail on this dataset, this consideration is not relevant here.

⁸We also explored evaluation of the models with a more complex measure called SLOR where we additionally normalized scores by word frequency (Pauls and Klein, 2012). Both metrics produced qualitatively similar results, so we only report the simpler metric here. See Appendix C.1.

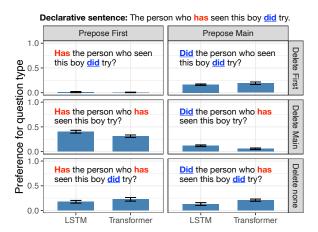


Figure 1: The question types that models prefer when offered a choice between 6 questions. These 6 questions are formed by modifying a declarative with a relative clause on the subject according to 'prepose' and 'delete' rules. The correct category is PREPOSE MAIN, DELETE MAIN. Within each architecture, the proportions across all 6 question types necessarily sum to 1. Each bar shows the average across 10 model re-runs, with single-standard-deviation error bars.

the most frequent preference was for PREPOSE FIRST, DELETE MAIN, a category that is only partially correct because it references linear order in addition to hierarchical structure (Figure 1).

Thus, neither model displays preferences consistent with the correct, fully-hierarchical generalization. The two model types showed similar scores, which may mean that these results are largely driven by the statistics of the training data that both models share, rather than the models' differing inductive biases.

One of the incorrect categories—PREPOSE MAIN, DELETE NONE, such as (6f)—only requires reference to hierarchical structure, so it could be said to capture the hierarchical nature of yes/no questions. Nonetheless, this category was also relatively rare: combining the two fully hierarchical possibilities (PREPOSE MAIN, DELETE MAIN and PREPOSE MAIN, DELETE NONE) accounts for only 26% of LSTM preferences and 27% of Transformer preferences, meaning that both models over 70% of the time favored a sentence generated at least partially based on linear order.

There are two likely reasons for why our models performed so poorly on yes-no questions when they performed well on many of the phenomena in the Zorro dataset (Section 4.5). First, yes/no questions may simply be harder to learn than the other phenomena; indeed, yes/no questions are often singled out as being likely to pose difficulties for a general-purpose learner (Section 1). While this focus in prior literature might simply be a historical coincidence, it is also possible that it points to a true difference in ease of learning. Alternatively, it might be that the six-way evaluation we used for yes/no questions is stricter than the binary judgments used for the Zorro dataset.

5 Experiment 2: Question Formation

The previous experiment was designed to operate entirely in the next-word-prediction paradigm, motivated by arguments from past literature about the strength and relative ecological validity of next-word-prediction as a training objective (see Section 4.2). However, one of this setup's shortcomings is that HIERARCHICALQ describes <u>correspondences</u> between questions and declaratives, but Experiment 1 focused on questions <u>alone</u>, with no consideration of declaratives.

In this second experiment, to better capture that HIERARCHICALQ is defined over sentence pairs, we trained models on a sentence-pair task: transforming a declarative into a question (McCoy et al., 2020). For instance, given *the child did learn* the model must produce *did the child learn* ?

We evaluated models in two ways. First, we checked if the models' predictions fully matched the correct questions. This full-sentence evaluation is demanding, and models might fail this evaluation for reasons unrelated to our core hypotheses. For instance, given *the child did learn* the model might produce *did the baby learn*, which would be marked as incorrect, even though this lexical error is not relevant to HIERARCHICALQ.

As a metric that is less demanding and that also more directly targets HIERARCHICALQ, we measured if the first word of the output question corresponded to the first or main auxiliary of the input. Critically, LINEARQ and HIERARCHICALQ make different predictions for the first word of a question so long as the two auxiliaries are distinct: see (4). Because this framing lets the model freely generate its output (instead of choosing one option from a pre-specified set), we allow for the possibility that the rule learned by models may not be identical to any of our manually-generated hypotheses.

Solely training models to perform this transformation involves the implicit assumption that, when children acquire English yes/no questions, the only evidence they leverage is English yes/no questions. However, other types of sentences may also provide useful evidence (Pearl and Mis, 2016): e.g., *wh*questions also illustrate subject-auxiliary inversion (Pullum and Scholz, 2002), while, more generally, many types of sentences could provide evidence that syntax as a whole is hierarchical (Perfors et al., 2011). To explore this possibility, we compared a condition in which models were only trained to perform question formation (the QUESTION FOR-MATION condition) to another in which models were first pre-trained on next-word prediction with the exact same setup as in Experiment 1 before being further trained to perform question formation (the NEXT-WORD PREDICTION + QUESTION FORMATION condition).

5.1 Dataset

Training Set Our question formation dataset consisted of the yes/no questions in the CHILDES Treebank (Pearl and Sprouse, 2013a,b), a parsed subset of CHILDES containing 189,359 sentences. We used these parses to extract all yes/no questions from the CHILDES Treebank and derive their corresponding declarative forms. The resulting declarative was concatenated with the question. An example declarative/question pair is:

 $(8) \ \ {\rm you} \ \ {\rm can} \ \ {\rm spell} \ \ {\rm your} \ \ {\rm name} \ . \ \ {\rm can} \ \ {\rm yous} \ \ {\rm spell} \ \ {\rm your} \ \ {\rm name} \ \ ?$

The training set consisted of 10,870 declarative/question pairs, the validation set 1,360 pairs, and the test set 1,358 pairs (we will call this test set the *randomly-partitioned test set* to distinguish it from two other evaluation sets discussed below). We trained models to perform next-word prediction on such concatenated sentence pairs.

The first-word accuracy of the trained model was then computed based on the model's prediction for the word after the period in each test example, while the full-sentence accuracy was computed based on its predictions for all tokens after the period. All questions in the randomly-partitioned test set were withheld from both the question-formation training set and the next-word-prediction training set. Thus, models had not seen these test examples in their training, even in the NEXT-WORD PRE-DICTION + QUESTION FORMATION condition in which they were trained on both tasks.

Evaluation Sets In addition to the randomlypartitioned test set, we used CFGs to generate two targeted evaluation sets. As in Experiment 1, we selected the CFGs' vocabulary from common words in our CHILDES data. In sentences generated from the first CFG, the sentence's first auxiliary was also its main auxiliary, so LINEARQ and HIERARCHI-CALQ make the same predictions. (9a) exemplifies the type of declarative-question pair in this dataset. We call this dataset FIRST-AUX = MAIN-AUX. For sentences generated by the second CFG, the main auxiliary was the *second* auxiliary in the sentence; thus, these examples disambiguate LINEARQ and HIERARCHICALQ. Example (9b) is a declarativequestion pair from this evaluation set. We call this dataset FIRST-AUX \neq MAIN-AUX. See Appendix F for the CFGs used.

(9) a. a girl was playing . was a girl playing ?b. a boy who is playing can try . can a boy who is playing try ?

5.2 Results

Randomly-Partitioned Test Set The LSTMs and Transformers in the QUESTION FORMA-TION condition performed well on the randomlypartitioned test set, with a full-question accuracy of 0.68 \pm 0.014 and 0.87 \pm 0.005 (averaged across 10 reruns with margins indicating one standard deviation). The models in the NEXT-WORD PRE-DICTION + QUESTION FORMATION condition performed similarly well, with a full-question accuracy of 0.66 \pm 0.008 for the LSTMs and 0.93 \pm 0.004 for the Transformers. For both model types, the first-word accuracy for the question was nearly 1.00 across re-runs. We suspect that Transformers have a stronger full-question accuracy because producing the question requires copying all words from the declarative (but in a different order). Copying is likely easy for Transformers because they can attend to specific words in the prior context, while our LSTMs must compress the entire context into a fixed-size vector, which may degrade the individual word representations. Because both model types achieved near-perfect performance on the crucial first-word accuracy metric, we conclude that our models have successfully learned how to handle the types of declarative/question pairs that we extracted from the CHILDES Treebank.

Targeted Evaluation Sets On our targeted evaluation sets, models seldom produced the complete question correctly. On the more lenient measure of first-word accuracy, for cases where LINEARQ and HIERARCHICALQ predict the same first output word (FIRST-AUX = MAIN-AUX), the Transformer trained only on question formation per-

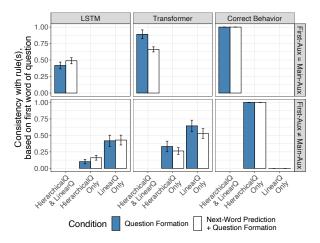


Figure 2: Proportion of model-produced or target questions that were consistent with the linear rule LINEARQ and/or the hierarchical rule HIERARCHICALQ. In the FIRST-AUX = MAIN-AUX dataset, the first auxiliary is the main auxiliary, so both LINEARQ and HIERARCHI-CALQ produce the correct question string. The FIRST-AUX \neq MAIN-AUX dataset disambiguates the two rules. Each bar in the LSTM and Transformer facets shows the average across 10 model re-runs, with error bars showing one standard deviation. The Correct Behavior column shows how a model would perform if it had perfectly learned the correct generalization.

formed strongly, while the Transformer trained on both tasks, and both LSTMs, performed decently (Figure 2; note chance performance is 1/vocabulary size, which is near 0.00). For cases that disambiguate the two rules (FIRST-AUX \neq MAIN-AUX), both models in both conditions performed more consistently with LINEARQ than HIERAR-CHICALQ. Training on next-word prediction before question formation had inconsistent effects: it modestly increased the chance of hierarchical behavior in LSTMs, and decreased it in Transformers.

Lexical Specificity In Appendix G, we further break down the FIRST-AUX \neq MAIN-AUX results based the auxiliaries' identity. The generalization pattern varied considerably across auxiliary pairs. For some auxiliary pairs, the auxiliary chosen to begin the question was usually neither auxiliary in the input (Figure 3, left facet). For other pairs, models usually chose the first auxiliary, regardless of lexical identity (Figure 3, middle facet). Finally, for some pairs, the auxiliary chosen was usually the same one, regardless of whether it was the first or main auxiliary (Figure 3, right facet).

Generalization based on lexical identity is rarely considered in past discussions of English yes/no question acquisition. Of the papers on this phe-

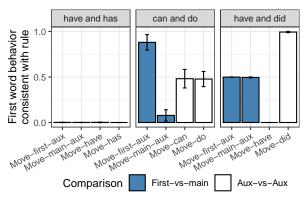


Figure 3: Lexical specificity in model behavior. Each facet considers only the evaluation examples containing the two auxiliaries in the facet heading; e.g., the *can and do* facet includes, for example, the inputs *the children who can play do learn* and *the children who do play can learn*. The bars show the proportion of model predictions for the first word of the output that are consistent with four potential movement rules, averaged across 10 model re-runs and with error bars showing one standard deviation above and below the mean. This plot only shows an illustrative subset of auxiliary pairs for one model type (Transformers in the NEXT-WORD PREDICTION + QUESTION FORMATION condition); see Appendix G for the full results.

nomenon (see Clark and Lappin (2010), Lasnik and Lidz (2017), and Pearl (2021) for overviews), the only one to our knowledge that discusses lexical specificity is Frank and Mathis (2007), which studied models trained on synthetic data. Our results highlight the importance of testing for a broad range of generalizations: Lexically-specific hypotheses appear attractive for our low-bias learners, so an account of what biases can yield human-like learning should rule out these lexically-specific hypotheses along with linear ones.

6 Discussion

We have found that, when trained on child-directed speech, two types of standard neural networks performed reasonably well at capturing the statistical properties of the dataset, yet their handling of English yes/no questions was more consistent with a linear rule LINEARQ than the correct hierarchical rule HIERARCHICALQ. These results support the hypothesis that a learner requires a hierarchical bias to consistently learn hierarchical rules when learning from the linguistic data children receive.

6.1 Takeaways for LSTMs and Transformers

When trained on massive corpora, LSTMs and Transformers perform impressively on some syn-

tactic evaluations. Based on such results, it is tempting to conclude that the general-purpose biases of these architectures suffice to yield human-like syntax acquisition. Our results caution against this interpretation: When we trained the same architectures on data more similar to children's input, they failed to learn the structure of English yes/no questions. Thus, at least when learning from text alone, LSTMs and Transformers do not display humanlike language learning—they do not generalize as humans do *from the data that humans receive*.

6.2 Takeaways for the Poverty of the Stimulus Debate

Below we specify four possible positions in the poverty-of-the-stimulus debate about the adequacy of children's input for inducing hierarchical rules in low-bias learners, arranged from assuming the most limited to the most expansive innate component:

- (10) **Any inductive biases:** Any learner trained on CHILDES will generalize like humans do.
- (11) Any inductive biases that enable indistribution learning: Any learner that captures the statistical patterns of the training distribution will generalize to HIERARCHICALQ.
- (12) **Some non-hierarchical inductive biases:** Some general-purpose learners will generalize as humans do, but others will not.
- (13) **Only a hierarchical inductive bias:** No general-purpose learners will generalize as humans do: hierarchical biases are necessary.

Position (10) is clearly false: many learners cannot learn certain aspects of syntax, no matter their training data (e.g., bigram models cannot capture long-distance dependencies). Our work shows that position (11) is also false: Though our models performed well on the in-distribution test sets of Experiments 1 and 2, they did not generalize in humanlike ways. This leaves positions (12) and (13), which our existing results cannot differentiate. It is possible that only learners with hierarchical inductive biases can demonstrate human-like language learning (position (13)), but also that some learners without this bias can succeed (position (12))—just not the learners we tested. For further discussion of how computational modeling can bear on learnability arguments, see Wilcox et al. (2022).

One potential solution supporting position (12) would be that learners leverage the hierarchical

structure of some syntactic phenomenon to help conclude that other, impoverished phenomena are hierarchical (Perfors et al., 2011; Mulligan et al., 2021). However, our results from Experiment 2 show that giving learners access to a wider range of phenomena does not automatically improve hierarchical generalization: Models' performance on question formation was not substantially improved (and in some cases was even harmed) when they were trained not just on question formation but also on next-word prediction on the entire CHILDES corpus. Thus, although training on text that contains many linguistic phenomena can give models a hierarchical inductive bias when the training is done over large Internet corpora (Warstadt and Bowman, 2020; Mueller et al., 2022), our results provide evidence that this conclusion does not extend to models trained on child-directed speech.

Though both (12) and (13) remain as possibilities, we believe that our results more strongly support (13). Of all currently available generalpurpose learners, LSTMs and Transformers are the best at modeling the probabilistic structure of linguistic data. Therefore, if child-directed speech contains clear evidence for the hierarchical nature of yes/no questions—evidence so clear that at least some general-purpose learners could recognize it it is likely that LSTMs and Transformers would be among the set of general-purpose learners that could use this evidence to make hierarchical generalizations in our experiments. The fact that these architectures instead predominantly favored linear generalizations therefore supports position (13).

6.3 How to test for HIERARCHICALQ

We have argued that an ideal simulation of the acquisition of English yes/no questions would have the following properties:

- (14) The training data should be similar to children's linguistic input.
- (15) The training task should be ecologically valid.
- (16) The evaluation method should focus on correspondences between pairs of sentences rather than the acceptability of individual sentences.

Property (14) motivated our use of text from CHILDES as the training data. We are not aware of a single experimental setup that fully satisfies both Property (15) and Property (16), so we instead used two experiments, each one focusing on one property at the cost of satisfying the other one less well. Experiment 1 works entirely in the context of the relatively ecologically valid task of nextword prediction, motivated by Property (15), but its evaluation is only based on the acceptability of individual sentences, failing to satisfy Property (16). Experiment 2 fully satisfies Property (16) by using an evaluation based on sentence pairs, at the cost of including a less ecologically-valid training component based on sentence transformations. Both experiments yielded qualitatively similar conclusions (failure of models to learn HIERARCHICALQ).

6.4 Quantity of Training Data

The size of our training set was plausibly in the range from which children can acquire HIERAR-CHICALQ. Crain and Nakayama (1987) found that children between ages 3 and 5 behaved much more consistently with HIERARCHICALQ than LINEARQ. Though these children made many errors, their errors were usually compatible with a hierarchical rule (e.g., PREPOSE MAIN, DELETE NONE errors: see Section 4.6). By age 3, American children receive approximately 10 to 33 million words of input (Hart and Risley, 1995), and the 8.5 million of our training set is near the lower end of that range. Thus, while we cannot be completely certain, it is reasonable to suppose that a learner that generalizes as children do would favor HIER-ARCHICALQ after being trained on our training set. Our models, in contrast, preferred sentences generated in ways based on linear order (Figures 1 and 2), a error category very rare in children (Crain and Nakayama, 1987; Ambridge et al., 2008).

In order to give our models the strongest chance of generalizing correctly, it would have been ideal to provide a quantity of data closer to 33 million words, the high end of Hart and Risley's range. Our data source did not contain enough text to make this possible, but future work could investigate ways to augment the data using other sources.

6.5 Type of Training Data

Our training set was both qualitatively and quantitatively closer to children's input than the massive Internet corpora standardly used to train models in NLP (Linzen, 2020). This difference is important: Lin et al. (2019), Warstadt and Bowman (2020), and Mueller et al. (2022) all found evidence that models trained on large Internet corpora performed well on yes/no questions evaluations, whereas our models trained on CHILDES performed poorly though we cannot be certain the differences in results are solely due to differences in the training data, since these prior papers used different model architectures, training tasks, and evaluation setups.

Though our training data are more similar to children's input than massive Internet corpora are, differences remain. Our experiments omit several aspects of a child's experience that might help them acquire syntax, such as prosody (Morgan and Demuth, 1996), visual information (Shi et al., 2019), meaning (Fitz and Chang, 2017; Abend et al., 2017), and social interaction (Kuhl et al., 2003; Rowe and Weisleder, 2020), all of which involve information that might correlate with syntactic structure and thus provide cues to the correct hierarchical generalization. On the other hand, our dataset might present an easier learning scenario than children are faced with, because children must learn to segment the speech stream into words (Lakhotia et al., 2021), while our models do not need to. Further, though real-world grounding could provide helpful information, learners might struggle to leverage this information due to difficulty determining what is being discussed in the physical world (Gleitman et al., 2005).

7 Conclusion

In this work, we trained two types of neural networks (LSTMs and Transformers) on sentences of the types available to children and then analyzed what they had learned about English yes/no questions. Across several evaluation paradigms, these models failed to generalize in human-like ways: Humans display hierarchical generalization, while the models' generalization was instead based on linear order and individual words' identities. Our results support the hypothesis that human-like linguistic generalization requires biases stronger than those of LSTMs and Transformers. Future work should investigate what inductive biases enable successful generalization. One approach would be to test architectures with built-in hierarchical structure; past work has shown that such architectures have a hierarchical bias (McCoy et al., 2020) and generalize better on the hierarchical phenomenon of subject-verb agreement (Kuncoro et al., 2018; Lepori et al., 2020), so they may also generalize better on English yes/no questions. A final direction would be to expand the input beyond words alone so that learners can leverage hierarchical structure that is present in other modalities, such as hierarchical structure in visual scenes.

Ethics Statement

Use of human data: While we did not collect any new human data ourselves, many of our analyses involved the use of prior datasets within the CHILDES database. All of these datasets were collected in accordance with IRB policies at the institutions of the data collectors, and all followed standard practices in obtaining informed consent and deidentifying data.⁹

Limitations

We view strong performance on our evaluation datasets as necessary but not sufficient to demonstrate human-like learning. Thus, if models perform poorly on our datasets (as the models we evaluated did), then we have strong reason to conclude that models are not learning in human-like ways. If future models perform better, such results would be consistent with human-like learning but would not conclusively establish that models learn as humans do, as they might instead be using some shallow heuristic that is not controlled for in our datasets. In other words, a criterion that is necessary but not sufficient facilitates strong conclusions about failure but does not facilitate strong conclusions about success. If future papers are faced with models that are more successful, such papers would ideally supplement results based on our datasets with analyses of models' internal strategies in order to more conclusively establish that what they have learned is not a spurious heuristic.

Thus an important risk of our proposed analyses is that future work using the same analyses might draw overly strong conclusions based on increased model performance, leading to overestimates of model strength. Such overestimates are an issue because they can lead users to place more trust in a model than is warranted.

Acknowledgments

For helpful comments and discussion, we are grateful to Najoung Kim, An Nguyen, Grusha Prasad, Paul Smolensky, Paul Soulos, and the NYU Computation and Psycholinguistics Lab. Any errors are our own. We are also grateful to the Maryland Advanced Research Computing Center (MARCC) for providing the computing resources used in our experiments. Portions of this research were supported by the National Science Foundation (NSF) under grants BCS-2114505, BCS-1919321, and Graduate Research Fellowship Program grant no. 1746891. Any opinions, findings, and conclusions or recommendations expressed in this material are those of the authors and do not necessarily reflect the views of the National Science Foundation.

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⁹https://talkbank.org/share/irb/

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A CHILDES preprocessing details

The train, test, and validation split kept each document in the corpora intact to allow for learning of context. Since a document roughly correspond to a single recording session, and the sentence order within each document was not randomized, the networks could utilize cross sentence context while predicting the next word.

Generally, we kept the data as close to the actual input that the child receives as possible. However, in some cases we modified tokenization to match the CHILDES Treebank, a syntactically parsed subset of the CHILDES corpora. For instance, contractions were split, e.g. we replaced *don't* with *do* n't,

The ages of the children vary by corpus, ranging from six months to twelve years. Almost 95% (49/52) of the corpora consist of transcriptions with children between one and six years of age.

Note that for Experiment 2, we used the same vocabulary as we used in Experiment 1, which means that the words that were not present in Experiment 1's vocabulary were replaced with <unk> tokens.

The unprocessed CHILDES datasets were downloaded in XML format from the online XML version¹⁰ of the CHILDES database (MacWhinney, 2000).¹¹ A modified NLTK CHILDESCorpus-Reader¹² was used to parse the XML into plain text for training.

The CHILDES dataset is licensed for use under a CC BY-NC-SA 3.0 license¹³. Under the terms of this license, the data can be freely used and adapted, as long as it is not used for commercial purposes and as long as attribution is provided.¹⁴ Our usage fits these criteria.

Though CHILDES contains many corpora of many languages, we use only corpora from the North American English subset of CHILDES, which contains child-directed speech with many different North American children. See the CHILDES database for more details.

By the CHILDES rules for data citation,¹⁵ research that relies on more than 6 of the corpora need only cite the overall database, not each individual corpus. All the data on CHILDES must adhere to IRB guidelines,¹⁶ including a requirement for anonymity.

The final dataset is included in our GitHub repository. This dataset is not intended for commercial use.

CHILDES corpora included The CHILDES corpora that we used were: Bates, Bernstein, Bliss, Bloom70, Bloom73, Bohannon, Braunwald, Brent, Brown, Carterette, Clark, Cornell, Demetras1, Demetras2, EllisWeismer, Evans, Feldman, Garvey, Gathercole, Gelman, Gillam, Gleason, HSLLD, Haggerty, Hall, Higginson, Kuczaj, MacWhinney, McCune, McMillan, Morisset, NH, Nelson, NewEngland, NewmanRatner, Normal, POLER, Peters, Post, Rollins, Sachs, Sawyer, Snow, Soderstrom, Sprott, Suppes, Tardif, Valian, VanHouten, VanKleeck, Warren, Weist.

B Hyperparameter Search and Model Implementation

We conducted a hyperparameter search for each of the architectures we investigated (LSTMs and Transformers). Our broad goal in this paper is to investigate the extent to which capturing the statistical properties of the CHILDES dataset naturally leads a learner to capture the structure of yes/no questions. Therefore, we sought to find the hyperparameter settings that made models most effective at capturing the statistical properties of CHILDES data, a goal which we operationalized as finding the model with the lowest perplexity.

B.1 Hyperparameter search

LSTMs For LSTMs we explored the following hyper-parameters via a grid search for a total of 144 models.

- 1. layers: 2
- 2. hidden and embedding size: 200, 800
- 3. batch size: 20, 80
- 4. dropout rate: 0.0, 0.2, 0.4, 0.6
- 5. learning rate: 5.0, 10.0, 20.0
- 6. random seed: 3 per parameter combination, unique for each LSTM

¹⁰https://childes.talkbank.org/data-xml/

¹¹https://childes.talkbank.org

¹²https://www.nltk.org/howto/childes.html

¹³https://talkbank.org/share/rules.html ¹⁴https://creativecommons.org/licenses/ by-nc-sa/3.0/

¹⁵https://talkbank.org/share/citation.html

¹⁶https://talkbank.org/share/irb/

The LSTM model with the lowest perplexity on the validation set after training had 2 layers, a hidden and embedding size of 800, a batch size of 20, a dropout rate of 0.4, and a learning rate of 10.¹⁷ A LSTM model with these hyperparameters has 37,620,294 parameters.

Transformers For the Transformers we performed a hyperparameter sweep over the following hyper-parameters for a total of 84 models.

- 1. layers: 2, 4, 8, 16
- 2. context size: 50, 100, 500
- 3. hidden and embedding size: 200, 800, 1600
- 4. heads: 2, 4, 8, 16
- 5. batch size: 20, 80, 160
- 6. dropout rate: 0.0, 0.2, 0.4, 0.6
- 7. learning rate: 0.5, 1.0, 5.0, 10.0, 20.0
- 8. random seed: 3 per parameter combination

The Transformer model with the lowest perplexities after training had 4 layers, a context size of 500, a hidden size of 800, a batch size of 10, 4 heads, a dropout rate of 0.2, and a learning rate of 5.0. A Transformer model with these parameters has 42,759,494 parameters.

We did not include a warmup period in our training procedure. In informal experiments, we tried including a warmup period for both LSTMs and Transformers, but we found that this did not meaningfully affect the perplexity of the trained models in our setting.

B.2 Comment on model size

Although neural networks generally perform better as they increase in size, the best-performing models that we found were not the largest ones. This result is consistent with the finding of Warstadt et al. (2020b) that, for small training sets, smaller language models sometimes outperform larger ones. Thus, it is unlikely that scaling up models beyond the range we investigated would have yielded better CHILDES language models than the ones we trained.

LSTMs	Prepose First	Prepose Main
Delete First	0.01	0.14
Delete Main	0.39	0.12
Delete None	0.20	0.14

Table 1: Numerical results for LSTMs' preference for questions consistent with combinations of 'prepose' and 'delete' rules. Within each architecture, the proportion preferences across all 6 question types necessarily sum to 1.

Transformers	Prepose First	Prepose Main
Delete First	0.01	0.16
Delete Main	0.31	0.06
Delete None	0.25	0.21

Table 2: Numerical results for Transformers' preference for questions consistent with combinations of 'prepose' and 'delete' rules. Within each architecture, the proportion preferences across all 6 question types necessarily sum to 1.

B.3 Implementation

All models were implemented in PyTorch by building on code from https://github.com/ facebookresearch/colorlessgreenRNNs and https://github.com/pytorch/examples/ tree/main/word_language_model, and trained using Nvidia k80 GPUs. The final models are included in our GitHub repository. These models are not intended for commercial use.

C PREPOSE-ONE & DELETE-ONE Full Results

See Table 1 and Table 2 for these results.

C.1 Results using SLOR

See Table 3 and Table 4 for these results.

LSTMs	Prepose First	Prepose Main
Delete First	0.01	0.14
Delete Main	0.33	0.08
Delete None	0.26	0.18

Table 3: Analysis of LSTMs' preference for questions consistent with combinations of 'prepose' and 'delete' rules, evaluated using SLOR. Within each architecture, the proportion preferences across all 6 question types necessarily sum to 1.

¹⁷The hyperparameters we explored for the LSTMs were those of Gulordava et al. (2018), the code for which can be found at https://github.com/facebookresearch/colorlessgreenRNNs

Transformers	Prepose First	Prepose Main
Delete First	0.01	0.15
Delete Main	0.27	0.04
Delete None	0.29	0.24

Table 4: Analysis of Transformers' preference for questions consistent with combinations of 'prepose' and 'delete' rules, evaluated using SLOR. Within each architecture, the proportion preferences across all 6 question types necessarily sum to 1.

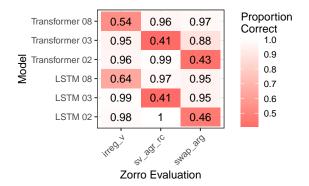


Figure 4: The performance of a selected subset of model re-runs on a selected subset of the Zorro evaluations. Each Zorro evaluation targets a specific syntactic phenomenon—in the cases shown here, irregular verbs, subject-verb agreement across relative clauses, and correct argument ordering.

D BabyBERTa dataset evaluation

For an illustrative subset of the results on the Zorro evaluation dataset (discussed in Section 4.5), see Figure 4. For the full results, see Figure 5.

E Move-One Dataset Results

One approach used in several past papers (e.g., Lewis and Elman (2001) and Reali and Christiansen (2005)) is to evaluate models using pairs of sentences that can be formed by starting with a declarative sentence (e.g., (17)) and moving one of its auxiliaries to the front of the sentence. The first sentence in each pair (e.g., (18a)) follows HIER-ARCHICALQ, because the *main* auxiliary is moved, while the second (e.g., (18b)), follows LINEARQ because the *first* auxiliary is moved.

- (17) The children who are talking are sleeping.
- (18) a. Are the children who are talking sleeping?b. Are the children who talking are sleeping?

If a model assigns a higher probability to (18a) than (18b), that is evidence that the models favors HIERARCHICALQ over LINEARQ. While this pref-

erence is a necessary component of correctly learning HIERARCHICALQ, it is by no means sufficient: indeed, Kam et al. (2008) showed that models can prefer sentences consistent with HIERARCHICALQ over sentences consistent with LINEARQ due to shallow *n*-gram statistics rather than due to knowledge of hierarchical structure. More generally, there are infinitely many other incorrect hypotheses besides LINEARQ, and demonstrating successful learning of HIERARCHICALQ would require ruling out all of them. Investigating all possibilities is intractable, but we can at least investigate a few additional plausible ones. Thus, in the main paper we depart from prior work by considering a greater number of candidate sentences than just the pairs of sentences used in prior work.

To create the MOVE-ONE dataset, we randomly sampled 10,000 declarative sentences from our CFGs for which the first and main auxiliary were identical and then modified them to give 10,000 sentence pairs. To create the PREPOSE-ONE&DELETE-ONE dataset, we randomly sampled a different 10,000 declarative sentences from our CFGs for which the first and main auxiliary were different and then we modified them to give 10,000 6-tuples of sentences. See Appendix F for more details about the CFGs.

F Context Free Grammars

Figure 6 contains the context-free grammar used for the analyses in Section 4.6. Figures 7 and 8 contain the context-free grammars used for the targeted evaluation sets in Section 5.2; for each of these evaluation sets, we sampled 10,000 declarative sentences from these grammars and transformed them into questions according to HIERARCHICALQ. Figure 9 contains the vocabulary used for all of these datasets.

G Breakdown by lexical identity

Here we further break down models' predictions for the FIRST-AUX \neq MAIN-AUX evaluation set based on the identities of the two auxiliaries in the input sentence. Figure 10 gives the results for the LSTM in the QUESTION FORMATION condition; Figure 11 for the LSTM in the NEXT-WORD PREDICTION + QUESTION FORMATION condition; Figure 12 for the Transformer in the QUES-TION FORMATION condition; and Figure 13 for the for the Transformer in the NEXT-WORD PREDIC-TION + QUESTION FORMATION condition.

	Transformer 10 -	42	53	86	74	63	88	76	80	93	90	53	63	94	83	99	86	96	96	75	82	55	50	53	
	Transformer 09 -	98	96	71	75	55	47	53	42	49	79	86	58	88	79	81	64	91	61	62	92	84	97	85	
	Transformer 08 -	91	67	64	96	83	98	81	100	97	72	79	54	40	58	40	54	80	71	60	92	83	69	38	
	Transformer 07 -	80	73	61	93	77	72	90	91	53	65	90	80	98	90	98	95	73	83	55	43	44	44	33	
	Transformer 06 -	74	76	53	44	55	42	47	80	72	59	90	78	72	87	92	58	66	96	80	99	88	98	94	
	Transformer 05 -	70	95	81	99	83	98	95	74	77	54	36	50	43	47	83	65	58	90	78	72	82	92	53	
	Transformer 04 -	60	88	75	74	61	92	51	63	95	84	100	88	98	93	73	80	53	38	78	42	53	83	73	
	Transformer 03 -	54	48	77	41	62	79	73	58	88	81	79	65	91	59	65	95	80	93	88	98	96	74	78	% Correct
	Transformer 02 -	82	97	83	99	94	71	78	54	43	72	45	48	85	71	59	96	80	74	58	91	62	62	93	
Model	Transformer 01 -	79	77	46	89	54	62	92	77	99	81	99	95	72	75	54	53	61	42	50	81	64	61	83	80
ω	LSTM 10 -	38	70	90	76	59	97	89	84	78	87	85	78	98	88	100	91	100	97	82	91	58	46	69	60
	LSTM 09 -	100	96	81	87	61	55	72	36	73	93	73	61	98	87	89	64	89	83	81	96	90	100	91	00
	LSTM 08 -	90	81	81	97	90	100	93	100	95	84	89	64	50	54	37	64	89	73	61	97	89	85	80	40
	LSTM 07 -	86	73	63	95	90	85	60	89	58	77	97	90	100	90	100	97	83	89	60	50	76	37	70	
	LSTM 06 -	84	89	61	53	51	36	61	89	74	62	99	88	83	89	88	79	80	98	90	99	93	100	94	
	LSTM 05 -	85	97	91	100	93	100	95	84	91	60	60	82	38	64	89	77	63	96	85	79	88	89	80	
	LSTM 04 -	61	98	87	88	85	88	80	82	97	90	100	93	99	96	83	86	59	43	48	39	68	90	73	
	LSTM 03 -	59	56	68	41	60	86	69	66	95	90	87	80	89	68	80	99	88	100	90	100	94	85	92	
	LSTM 03 - LSTM 02 -		56 100			60 96	85	69 88	61	95 46	39	39	80 74	88	68 78	59	99 98	88 88	100 88	90 62	100 89	94 79	83	98	
		89		91 67		96 86	85 82		<mark>61</mark> 91		39	39				59 60	98 56	88 78	88 40	62 67			83 59		
	LSTM 02 -	89	100	91	100	96	85	88	61	46	39	binding-principle_a - 001	74	ellipsis-n_bar - <mark>58</mark>	78	59	98	88	88	62	89	79	83	98	

Figure 5: Results on the targeted syntactic evaluations in Huebner et al. (2021) in percent accuracy. Evaluation names in Figure 4 were shortened.

H Example generated text

Figure 14 gives some example text generated by our models. Models trained on next-word prediction produce their predictions as a probability distribution over the vocabulary. To use such models to generate text, we sample a word from this distribution then use that word as the model's input for the next time step.

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$\begin{array}{lll} NP_S & \rightarrow \{ Det_S N_S \} \\ NP_P & \rightarrow \{ Det_P N_P \} \\ NP_O & \rightarrow \{ Det_S N_S \mid Det_P N_P \mid Det_S N_S Det_S N_S \mid Det_S N_S Pep Det_P N_P Det_P N_P Det_P N_P Prep Det_S N_S \mid Det_P N_P Prep Det_P N_P \} \\ VP_S_BARE & \rightarrow \{ Aux_S IV \} \\ VP_S_BARE & \rightarrow \{ Aux_S TV NP_O \} \\ VP_S_PROG & \rightarrow \{ Aux_S BE IV_IS \} \\ VP_S_PROG & \rightarrow \{ Aux_S BE TV_IS NP_O \} \\ VP_S_PROG & \rightarrow \{ Aux_S_BE TV_IS NP_O \} \\ VP_S_PAST & \rightarrow \{ Aux_S_HAS TV_HAS \} \\ VP_S_PAST & \rightarrow \{ Aux_P TV \} \\ VP_P_BARE & \rightarrow \{ Aux_P TV \} \\ VP_P_BARE & \rightarrow \{ Aux_P TV NP_O \} \\ VP_P_PROG & \rightarrow \{ Aux_P TV NP_O \} \\ VP_P_PROG & \rightarrow \{ Aux_P TV NP_O \} \\ VP_P_PROG & \rightarrow \{ Aux_P_BE TV_IS NP_O \} \\ VP_P_PROG & \rightarrow \{ Aux_P_BE TV_IS \} \\ VP_P_PROG & \rightarrow \{ Aux_P_BE TV_IS \} \\ VP_P_PAST & \rightarrow \{ Aux_P_HAS TV_HAS \} \\ VP_P_PAST & \rightarrow \{ Rel Aux_S IV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_S_SE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Det_S N_S Aux_S_S TV_IAS \\ RC_S_PROG & \rightarrow \{ Rel Aux_S_IV_IS \mid Rel Aux_S_SE TV_IS \mid Rel Aux_S_SE TV_IS \mid Rel Aux_S_SE TV_IS \mid Rel Aux_S_S S N_S \mid Rel Aux_S_S S N_S \mid Rel Aux_S_SE TV_IS \mid Rel Aux_S_S S N_S \mid Rel Aux_S_SE TV_IS \mid Rel Aux_S_S S N_S N_S N_S N_S N_S N_S N_S N_S N$	S	\rightarrow {NP_P RC_P_PAST MAIN-AUX VP_P_PROG}
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$\begin{array}{lll} \label{eq:prod} & \rightarrow \{ \operatorname{Aux} S_BE \mathrm{TV}_{IS} \mathrm{NP}_O \} \\ \end{tabular} \\ tab$		
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$\begin{array}{lll} \label{eq:product} VP_S_PAST & \rightarrow \{Aux_S_HAS TV_HAS NP_O\} \\ VP_P_BARE & \rightarrow \{Aux_P TV NP_O\} \\ VP_P_BARE & \rightarrow \{Aux_P TV NP_O\} \\ VP_P_PROG & \rightarrow \{Aux_P_BE TV_IS NP_O\} \\ VP_P_PROG & \rightarrow \{Aux_P_BE TV_IS NP_O\} \\ VP_P_PAST & \rightarrow \{Aux_P_HAS TV_HAS NP_O\} \\ VP_P_PAST & \rightarrow \{Aux_P_HAS TV_HAS NP_O\} \\ RC_S_BARE & \rightarrow \{Rel Aux_S IV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S_SE TV_IS \mid Rel Det_P N_P] \\ RC_S_PROG & \rightarrow \{Rel Aux_S_BE IV_IS \mid Rel Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Aux_S_BE TV_IS Det_P N_P] \\ RC_S_PAST & \rightarrow \{Rel Aux_S_HAS IV_HAS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_S N_S Aux_S_SBE TV_IS \mid Rel Aux_S_BE TV_IS Det_P N_P] \\ RC_P_BARE & \rightarrow \{Rel Aux_P_IV IV \mid Rel Det_S N_S Aux_S_TV_IS IRel Aux_P_TV \mid Rel Aux_P_TV_IS \mid Rel Aux_S_TV_IS N_S \mid Rel Aux_S_TV_IS N_S \mid Rel Aux_S_TV_IS N_S \mid Rel Aux_S_DE TV_IS \mid Rel Det_S N_S Aux_S_TV_TV_IS \mid Rel Aux_S_TV_IS N_S \mid Rel Aux_P_TV_IS \mid Rel Aux_P_TV_IS \mid Rel Det_P N_P_Aux_P_TV \mid Rel Aux_P_TV_IS \mid Rel Aux_P_TV_IS \mid Rel Aux_S_TV_IS \mid Rel Aux_P_TV_IS \mid Rel Aux_S_TV_IS \mid Rel Aux_P_TV_IS \mid RE Aux_P_TV_IS \mid ReL Aux_P_TV_IS \mid RE Aux_P_TV_IS \mid ReL Aux_P_TV_IS \mid RE Aux_P_TV_IS \mid RE Aux_P_TV_IS \mid RE Aux_P_TV_IS \mid RE Aux_P_TV_IS _RC_P_RS N_S \mid ReL Aux_P_TV_IS \mid RE Aux_P_TS _S RE TV_IS \mid RE Aux_P_TS _TV_IS _RC_P_RS RC_P_P_RS RC_P_P_RS RC_P_P_RS RC_P_P_S RC_P_P_RS RC_P_P_S RC_P_P_RS$		
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$\begin{array}{lll} VP_P_PROG & \rightarrow \{Aux_P_BE IV_IS\} \\ VP_P_PROG & \rightarrow \{Aux_P_BE TV_IS NP_O\} \\ VP_P_PROG & \rightarrow \{Aux_P_BE TV_IS NP_O\} \\ VP_P_PAST & \rightarrow \{Aux_P_HAS TV_HAS NP_O\} \\ RC_S_BARE & \rightarrow \{Rel Aux_S TV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S TV Det_P N_P\} \\ RC_S_PROG & \rightarrow \{Rel Aux_S_BE IV_IS \mid Rel Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_HAS TV_HAS \mid Rel Aux_S_HAS TV_HAS \mid Rel Det_P N_P \\ RC_S_PAST & \rightarrow \{Rel Aux_S_HAS IV_HAS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_HAS TV_HAS \mid Rel Aux_S_HAS TV_HAS Det_S N_S \mid Rel Aux_P_TV \mid Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_TV \mid Rel Aux_P_TV \mid RE Aux_P_TV \mid Rel Aux_P_TV \mid Rel Aux_P_TV \mid Rel Aux_P_TV_S \mid RE TV_S \mid RE _TV_S \mid RE _TV_S _TV_S \mid RE _T$		
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$\begin{array}{ll} VP_P_PAST & \rightarrow \{Aux_P_HAS IV_HAS\} \\ VP_P_PAST & \rightarrow \{Aux_P_HAS TV_HAS NP_O\} \\ RC_S_BARE & \rightarrow \{Rel Aux_S IV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S TV Det_P N_P\} \\ RC_S_PROG & \rightarrow \{Rel Aux_S_BE IV_IS \mid Rel Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Aux_S_BE TV_IS Det_S N_S \mid Rel Aux_S_BE TV_IS Det_P N_P] \\ RC_S_PAST & \rightarrow \{Rel Aux_S_HAS IV_HAS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_HAS TV_HAS \mid Rel Aux_S_HAS TV_HAS Det_S N_S \mid Rel Aux_P_TV \mid Rel Aux_P_TV_IS \mid Rel Aux_P_RE TV_IS \mid RE TV_IS \mid RE TV_IS \mid RE Aux_P_RE TV_IS _RE TV_IS \mid RE Aux_P_RE TV_IS _RE TV_IS _RE TV_IS \mid RE Aux_P_RE TV_IS \mid RE Aux_P_RE TV_IS _RE $		
$\begin{array}{lll} VP_PAST & \rightarrow \{Aux_P_HAS TV_HAS NP_O\} \\ RC_S_BARE & \rightarrow \{Rel \ Aux_S \ IV \ \ Rel \ Det_S \ N_S \ Aux_S \ TV \ \ Rel \ Det_P \ N_P \ Aux_P \ TV \ \ Rel \ Aux_S \ TV \ Det_S \ N_S \ \ Rel \ Aux_S \ TV \ Det_S \ N_S \ \ Rel \ Det_P \ N_P \ Aux_P \ TV_IS \ \ Rel \ Det_S \ N_S \ Aux_S \ S \ LS \ S \ Aux_S \ S \ S \ Rel \ Aux_S \ S \ Rel \ Aux_S \ TV \ Det_S \ N_S \ Rel \ Aux_S \ S \ S \ Rel \ Aux_S \ Rel \ R$		
$\begin{array}{lll} RC_S_BARE & \rightarrow \{ Rel Aux_S IV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_S TV Det_S N_S \mid Rel Aux_S TV Det_P N_P \} \\ RC_S_PROG & \rightarrow \{ Rel Aux_S_BE IV_IS \mid Rel Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Aux_S_BE TV_IS Det_S N_S \mid Rel Aux_S_BE TV_IS Det_P N_P \} \\ RC_S_PAST & \rightarrow \{ Rel Aux_S_HAS IV_HAS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_HAS TV_HAS \mid Rel Aux_S_HAS TV_HAS Det_S N_S Rel Aux_P_TV \mid Rel Aux_S_HAS TV_HAS Det_P N_P \} \\ RC_P_BARE & \rightarrow \{ Rel Aux_P_IV \mid Rel Det_S N_S Aux_S_TV_IS \mid Rel Det_P N_P Aux_P_TV \mid Rel Aux_P_BE TV_IS \mid Rel Aux_P_TV \mid S \mid Rel Aux_P_TU \mid S \mid Rel Aux_P_TV \mid S \mid Rel Aux_P_TU \mid S \mid Re Au$		
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$\begin{array}{llllllllllllllllllllllllllllllllllll$	RC S PROG	
$\begin{array}{llllllllllllllllllllllllllllllllllll$		
$ \begin{array}{ll} RC_S_PAST & \rightarrow \{ Rel \ Aux_S_HAS \ IV_HAS \ \ Rel \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ \ Rel \ Det_P \ N_P \ Aux_P_HAS \ TV_HAS \ \ Rel \ Aux_S_HAS \ TV_HAS \ Det_S \ N_S \ \ Rel \ Aux_S_HAS \ TV_HAS \ Det_P \ N_P \ Aux_P \ TV \ \ Rel \ Aux_P \ TV \ Det_S \ N_S \ Aux_S \ TV \ \ Rel \ Det_P \ N_P \ Aux_P \ TV \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Aux_S_HAS \ TV_HAS \ Rel \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Aux_S_HAS \ TV_HAS \ Rel \ Det_P \ N_P \ Aux_P_BE \ TV_HAS \ Aux_S_BE \ TV_HAS \ Aux_S_BE \ TV_HAS \ Rel \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_P_BE \ TV_IS \ Aux_S_BE \ TV_S \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_IS \ Aux_S_BE \ TV_S \ Aux_S_BE \ Aux_S_BE \ TV_S \ Aux_S_BE \ Aux_S_BE \ TV_S \ Aux_S_BE \ TV_S \ Aux_S_BE \ Aux_S_BE \ TV_S \ Aux_S_BE \ Aux_$		
$\begin{array}{llllllllllllllllllllllllllllllllllll$	RC S PAST	
$\begin{array}{ll} Rel Aux_S_HAS TV_HAS Det_P N_P \\ RC_P_BARE & \rightarrow \{Rel Aux_P IV \mid Rel Det_S N_S Aux_S TV \mid Rel Det_P N_P Aux_P TV \mid Rel Aux_P TV Det_S N_S \mid Rel Aux_P TV Det_P N_P \\ RC_P_PROG & \rightarrow \{Rel Aux_P_BE IV_IS \mid Rel Det_S N_S Aux_S_BE TV_IS \mid Rel Det_P N_P Aux_P_BE TV_IS \mid Rel Aux_P_BE TV_IS Det_S N_S \mid Rel Aux_P_BE TV_IS Det_S N_S \mid Rel Aux_P_BE TV_IS \mid Rel Det_S N_S Aux_S_HAS TV_HAS \mid Rel Det_P N_P Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS Det_S N_S \mid Rel Aux_P_HAS TV_HAS \mid Rel Aux_P_HAS TV_HAS TV_TT TTTTTTTTTTTTTTTTTTTTTTTTTTTTTTTT$		
$ \begin{array}{ll} RC_P_BARE & \rightarrow \{ Rel \ Aux_P \ IV \ \ Rel \ Det_S \ N_S \ Aux_S \ TV \ \ Rel \ Det_P \ N_P \ Aux_P \ TV \ \ Rel \ Aux_P \ TV \ Det_S \ N_S \ \ Rel \ Aux_P \ TV \ Det_P \ N_P \ Aux_P \ TV \ Det_S \ N_S \ \ Rel \ Aux_P \ TV \ Det_S \ N_S \ Aux_S \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ Aux_S \ Aux_S \ Aux_S \ TV_HAS \ I \ Rel \ Aux_P_BE \ TV_HAS \ I \ Rel \ Aux_P_Aux_P_BE \ TV_HAS \ I \ Rel \ Aux_P_Aux_S \ TV_HAS \ I \ Rel \ Aux_P_Aux_S \ Aux_S \ Au$		
$ \begin{array}{ll} Rel \ Aux_P \ TV \ Det_S \ N_S \ \ Rel \ Aux_P \ TV \ Det_P \ N_P \\ \hline RC_P_PROG & \rightarrow \{ Rel \ Aux_P_BE \ IV_IS \ \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ \ Rel \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \\ \hline TV_IS \ Det_P \ N_P \\ \hline RC_P_PAST & \rightarrow \{ Rel \ Aux_P_HAS \ IV_HAS \ \ Rel \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ I \ Rel \ Aux_P_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ Rel \ Aux_P_HAS \ TV_HAS \ TV_HAS \ Rel \ Aux_P_HAS \ TV_HAS \ Rel \ Aux_P_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ TV_HAS \ TV_HAS \ TV_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ Aux_P_HAS \ TV_HAS \ TV_HAS \ TV_HAS $	RC P BARE	,
$ \begin{array}{ll} RC_P_PROG & \rightarrow \{ Rel \ Aux_P_BE \ IV_IS \ \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ \ Rel \ Det_P \ N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_S \ N_S \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ Aux_P_HAS \ IV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ IRel \ Aux_P_HAS \ TV_HAS \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ Det_S \ N_S \ Aux_P_HAS \ TV_HAS \ IRel \ Aux_P_HAS \ TV_HAS \ Det_S \ N_S \ Aux_P_HAS \ Aux_P_Aux_P_Aux_P_Aux_P_Aux_P_Aux_P_Aux_P_Aux_P_$		
$\begin{array}{l} N_P \ Aux_P_BE \ TV_IS \ \ Rel \ Aux_P_BE \ TV_IS \ Det_S \ N_S \ \ Rel \ Aux_P_BE \ TV_IS \ Det_P \ N_P \ \\ RC_P_PAST & \rightarrow \{ Rel \ Aux_P_HAS \ IV_HAS \ \ Rel \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ \ Rel \ Det_P \ N_P \ Aux_P_HAS \ TV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ Det_S \ N_S \ \\ \end{array}$	RC P PROG	
$ \begin{array}{l} TV_IS \ Det_P \ N_P \\ RC_P_PAST \end{array} \rightarrow \{ Rel \ Aux_P_HAS \ IV_HAS \ \ Rel \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ \ Rel \ Det_P \ N_P \ Aux_P_HAS \ TV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ Det_S \ N_S \ \\ \end{array} $		
$ \begin{array}{ll} RC_P_PAST & \rightarrow \{ Rel \ Aux_P_HAS \ IV_HAS \ \ Rel \ Det_S \ N_S \ Aux_S_HAS \ TV_HAS \ \ Rel \ Det_P \ N_P \ Aux_P_HAS \ TV_HAS \ \ Rel \ Aux_P_HAS \ TV_HAS \ Det_S \ N_S \ Aux_P_HAS \ Det_S \ N_S \ Aux_P_HAS \ Aux_P_Aux$		
Det_P N_P Aux_P_HAS TV_HAS Rel Aux_P_HAS TV_HAS Det_S N_S	RC P PAST	
	i _i/.01	

Figure 6: CFG used to generate PREPOSE-ONE-AND-DELETE-ONE evaluation dataset

- $S \longrightarrow \{NP_M_S VP_M_S \mid NP_M_P VP_M_P\}$
- $NP_M_S \rightarrow \{ Det_S \ N_S \ | \ Det_S \ N_S \ Prep \ Det_S \ N_S \ Prep \ Det_P \ N_P \}$
- $NP_M_P \rightarrow \{Det_P N_P \mid Det_P N_P Prep Det_S N_S \mid Det_P N_P Prep Det_P N_P\}$
- - $N_S RC_S | Det_P N_P RC_P \}$
- $VP_M_S \rightarrow \{Aux_S IV\}$
- $VP_M_S \rightarrow \{Aux_S \; TV \; NP_O\}$
- $VP_M_S \rightarrow \{Aux_S_BE \; IV_IS\}$
- $VP_M_S \rightarrow \{Aux_S_BE \ TV_IS \ NP_O\}$
- $VP_M_S \rightarrow {Aux_S_HAS IV_HAS}$
- $VP_M_S \rightarrow \{Aux_S_HAS \ TV_HAS \ NP_O\}$
- $VP_M_P \rightarrow \{Aux_P IV\}$
- $VP_M_P \rightarrow \{Aux_P \ TV \ NP_O\}$
- $VP_M_P \rightarrow \{Aux_P_BE\ IV_IS\}$
- $VP_M_P \rightarrow \{Aux_P_BE \ TV_IS \ NP_O\}$
- $VP_M_P \rightarrow \{Aux_P_HAS IV_HAS\}$
- $VP_M_P \rightarrow \{Aux_P_HAS \ TV_HAS \ NP_O\}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel Aux_S \ IV \ | \ Rel \ Det_S \ N_S \ Aux_S \ TV \ | \ Rel \ Det_P \ N_P \ Aux_P \ TV \ | \\ Rel \ Aux_S \ TV \ Det_S \ N_S \ | \ Rel \ Aux_S \ TV \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel \ Aux_S_BE \ IV_IS \ | \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ | \ Rel \ Det_P \\ & N_P \ Aux_P_BE \ TV_IS \ | \ Rel \ Aux_S_BE \ TV_IS \ Det_S \ N_S \ | \ Rel \ Aux_S_BE \\ & TV_IS \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel \: Aux_S_HAS \: IV_HAS \: | \: Rel \: Det_S \: N_S \: Aux_S_HAS \: TV_HAS \: | \: Rel \: Det_P \: N_P \: Aux_P_HAS \: TV_HAS \: | \: Rel \: Aux_S_HAS \: TV_HAS \: Det_S \: N_S \: | \: Rel \: Aux_S_HAS \: TV_HAS \: Det_P \: N_P \} \end{array}$
- $\begin{array}{ll} \text{RC}_P & \rightarrow \{ \text{Rel Aux}_P \text{ IV} \mid \text{Rel Det}_S \text{ N}_S \text{ Aux}_S \text{ TV} \mid \text{Rel Det}_P \text{ N}_P \text{ Aux}_P \text{ TV} \mid \\ & \text{Rel Aux}_P \text{ TV} \text{ Det}_S \text{ N}_S \mid \text{Rel Aux}_P \text{ TV} \text{ Det}_P \text{ N}_P \} \end{array}$
- $\begin{array}{ll} RC_P & \rightarrow \{ Rel \ Aux_P_BE \ IV_IS \ | \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ | \ Rel \ Det_P \\ & N_P \ Aux_P_BE \ TV_IS \ | \ Rel \ Aux_P_BE \ TV_IS \ Det_S \ N_S \ | \ Rel \ Aux_P_BE \\ & TV_IS \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_P & \rightarrow \{ Rel \: Aux_P_HAS \: IV_HAS \mid Rel \: Det_S \: N_S \: Aux_S_HAS \: TV_HAS \mid Rel \: Det_P \: N_P \: Aux_P_HAS \: TV_HAS \mid Rel \: Aux_P_HAS \: TV_HAS \: Det_S \: N_S \mid Rel \: Aux_P_HAS \: TV_HAS \: Det_P \: N_P \} \end{array}$

Figure 7: CFG used to generate FIRST-AUX = MAIN-AUX evaluation dataset

- $S \longrightarrow \{NP_M_S VP_M_S \mid NP_M_P VP_M_P\}$
- $NP_M_S \rightarrow \{ Det_S \ N_S \ | \ Det_S \ N_S \ Prep \ Det_S \ N_S \ Prep \ Det_P \ N_P \}$
- $NP_M_P \rightarrow \{Det_P N_P \mid Det_P N_P Prep Det_S N_S \mid Det_P N_P Prep Det_P N_P\}$
- - $N_S RC_S | Det_P N_P RC_P \}$
- $VP_M_S \rightarrow \{Aux_S IV\}$
- $VP_M_S \rightarrow \{Aux_S \ TV \ NP_O\}$
- $VP_M_S \rightarrow \{Aux_S_BE \; IV_IS\}$
- $VP_M_S \rightarrow \{Aux_S_BE \ TV_IS \ NP_O\}$
- $VP_M_S \rightarrow {Aux_S_HAS IV_HAS}$
- $VP_M_S \rightarrow \{Aux_S_HAS \ TV_HAS \ NP_O\}$
- $VP_M_P \rightarrow \{Aux_P IV\}$
- $VP_M_P \rightarrow \{Aux_P \; TV \; NP_O\}$
- $VP_M_P \rightarrow \{Aux_P_BE\ IV_IS\}$
- $VP_M_P \rightarrow \{Aux_P_BE \ TV_IS \ NP_O\}$
- $VP_M_P \rightarrow \{Aux_P_HAS IV_HAS\}$
- $VP_M_P \rightarrow \{Aux_P_HAS \ TV_HAS \ NP_O\}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel Aux_S \ IV \ | \ Rel \ Det_S \ N_S \ Aux_S \ TV \ | \ Rel \ Det_P \ N_P \ Aux_P \ TV \ | \\ Rel \ Aux_S \ TV \ Det_S \ N_S \ | \ Rel \ Aux_S \ TV \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel \ Aux_S_BE \ IV_IS \ | \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ | \ Rel \ Det_P \\ & N_P \ Aux_P_BE \ TV_IS \ | \ Rel \ Aux_S_BE \ TV_IS \ Det_S \ N_S \ | \ Rel \ Aux_S_BE \\ & TV_IS \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_S & \rightarrow \{ Rel \: Aux_S_HAS \: IV_HAS \: | \: Rel \: Det_S \: N_S \: Aux_S_HAS \: TV_HAS \: | \: Rel \: Det_P \: N_P \: Aux_P_HAS \: TV_HAS \: | \: Rel \: Aux_S_HAS \: TV_HAS \: Det_S \: N_S \: | \: Rel \: Aux_S_HAS \: TV_HAS \: Det_P \: N_P \} \end{array}$
- $\begin{array}{ll} \text{RC}_P & \rightarrow \{ \text{Rel Aux}_P \text{ IV} \mid \text{Rel Det}_S \text{ N}_S \text{ Aux}_S \text{ TV} \mid \text{Rel Det}_P \text{ N}_P \text{ Aux}_P \text{ TV} \mid \\ & \text{Rel Aux}_P \text{ TV} \text{ Det}_S \text{ N}_S \mid \text{Rel Aux}_P \text{ TV} \text{ Det}_P \text{ N}_P \} \end{array}$
- $\begin{array}{ll} RC_P & \rightarrow \{ Rel \ Aux_P_BE \ IV_IS \ | \ Rel \ Det_S \ N_S \ Aux_S_BE \ TV_IS \ | \ Rel \ Det_P \\ & N_P \ Aux_P_BE \ TV_IS \ | \ Rel \ Aux_P_BE \ TV_IS \ Det_S \ N_S \ | \ Rel \ Aux_P_BE \\ & TV_IS \ Det_P \ N_P \} \end{array}$
- $\begin{array}{ll} RC_P & \rightarrow \{ Rel \: Aux_P_HAS \: IV_HAS \mid Rel \: Det_S \: N_S \: Aux_S_HAS \: TV_HAS \mid Rel \: Det_P \: N_P \: Aux_P_HAS \: TV_HAS \mid Rel \: Aux_P_HAS \: TV_HAS \: Det_S \: N_S \mid Rel \: Aux_P_HAS \: TV_HAS \: Det_P \: N_P \} \end{array}$

Figure 8: CFG used to generate FIRST-AUX \neq MAIN-AUX evaluation dataset

Det_S	\rightarrow {the some this }
Det_P	\rightarrow {the some those}
N_S	\rightarrow {baby girl boy animal child person horse }
N_P	\rightarrow {babies girls boys animals children people horses }
IV	\rightarrow {play read draw sit fall talk sleep try work walk}
IV_IS	\rightarrow {playing reading drawing sitting falling talking sleeping trying
	working walking}
IV_HAS	\rightarrow {played read drawn sat fallen talked slept tried worked walked}
TV	\rightarrow {call see find help feed know pick visit watch reach}
TV_IS	\rightarrow {calling seeing finding helping feeding knowing picking visiting
	watching reaching}
TV_HAS	\rightarrow {called seen found helped fed known picked visited watched
	reached}
Aux_P	\rightarrow {do did can would shall}
Aux_S	\rightarrow {does did can would shall}
Aux_S_BE	$E \rightarrow \{is \mid was\}$
Aux_P_BE	$E \rightarrow \{are \mid were\}$
Aux_S_HA	$AS \rightarrow \{has\}$
Aux_P_HA	$AS \rightarrow \{have\}$
Prep	\rightarrow {by behind }
Rel	\rightarrow {who that }

Figure 9: Vocabulary used for the PREPOSE-ONE-AND-DELETE-ONE, FIRST-AUX \neq MAIN-AUX, and FIRST-AUX = MAIN-AUX evaluation datasets

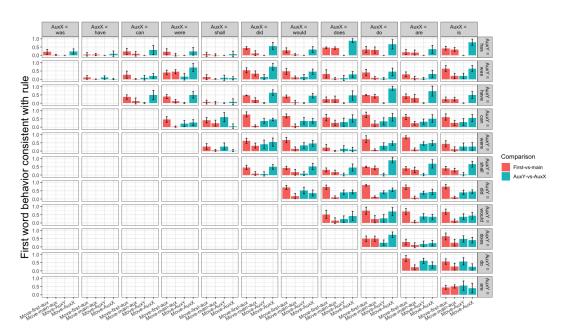


Figure 10: Breakdown by the identities of the two auxiliaries for outputs in the FIRST-AUX \neq MAIN-AUX evaluation set for LSTMs trained only on question formation. The two leftmost bars in each cell show a First-vs-main comparison, while the two rightmost bars show an AuxY-vs-AuxX comparison.

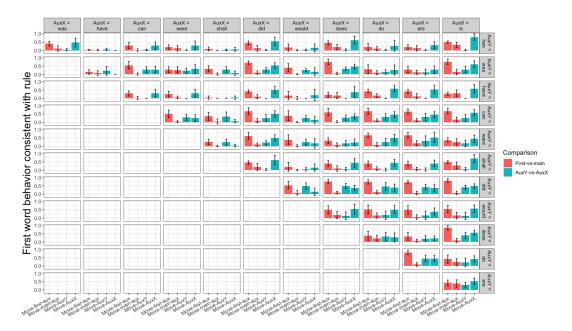


Figure 11: Breakdown by the identities of the two auxiliaries for outputs in the FIRST-AUX \neq MAIN-AUX evaluation set for LSTMs first trained on next-word prediction and then question formation. The two leftmost bars in each cell show a First-vs-main comparison, while the two rightmost bars show an AuxY-vs-AuxX comparison.

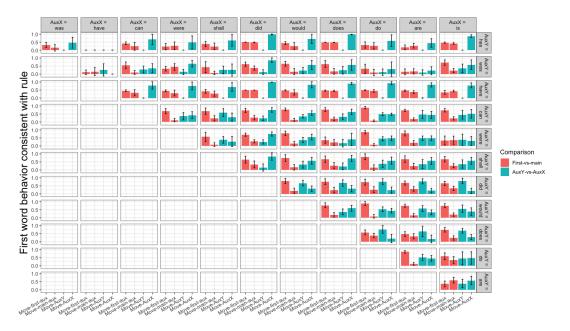


Figure 12: Breakdown by the identities of the two auxiliaries for outputs in the FIRST-AUX \neq MAIN-AUX evaluation set for Transformers trained only on question formation. The two leftmost bars in each cell show a First-vs-main comparison, while the two rightmost bars show an AuxY-vs-AuxX comparison.

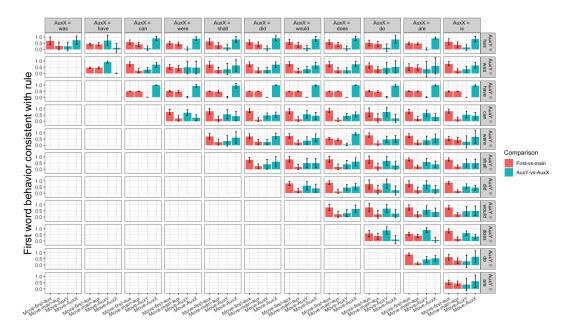


Figure 13: Breakdown by the identities of the two auxiliaries for outputs in the FIRST-AUX \neq MAIN-AUX evaluation set for Transformers first trained on next-word prediction and then question formation. The two leftmost bars in each cell show a First-vs-main comparison, while the two rightmost bars show an AuxY-vs-AuxX comparison.

Text from CHILDES	do you eat in nursery school too ? oh . it 's nursery school . xxx . what do you get to eat ? what else do you get to eat besides a book ? do n't play with those books . what else do you have ? what do you have in nursery school ? alright - you can take it . why do n't you put the turtle back . well - you 're not going to change his water now . tonight . tonight - you change it about ten times a day . no - you can do it later . forget it now . too bad . too bad . that poor turtle . you do n't let him sit there five minutes . that was five minutes ?
LSTM gen- erated text	do you eat in nursery school too ? oh . it 's nursery school . no ! tomorrow 's Friday . right . yeah - yeah . yeah I know what . I told you that he liked snipsnap that way . well this is address the grayish kings . ok . what kind of bird do you want to play with ? what else do you want to do ? your crayons . got a circle . I 'm going to use these . there . remember ? ok do you want to put all of these there ? ok let 's put everything away . what do you want to do ? you want to play in the box ? it 's just like a ball because it has a ball on it .
Transformer	do you eat in nursery school too? oh. it 's nursery school. mm-hm. and it
generated	looks like a little girl . mm-hm . like a little girl . hm , mm-hm . looks like she
text	's concerned about baseball this is a picture of a double football player . mm-hm . um, it has a uniform on it . mm-hm . anything more ? no . ok great . got a hat on . and a flower and a little flower . remember that ? do you remember that word ? what do you remember that word ? do you remember what it word says ? it says seven - eight . what 's that word ? it says eight . look at that word . three - four - six eight - nine

Figure 14: Comparison of text generated by the LSTM and Transformer models with a block of text chosen randomly from the training data. The LSTMs and Transformers were both prompted with the first three sentences of the text taken from CHILDES, which is the underlined in the two model generated texts. Note that neither of the model generated texts were cherry-picked either for quality or to be representative of the models' usual output: rather they were the first things they generated when prompted with the above underlined portion.